

$$16. \frac{\frac{1}{x+1} - 1}{\frac{1}{x-1} + 1}$$

find the LCD

$$\text{LCD} = \underline{(x+1)(x-1)}$$

$$\frac{(x+1)(x-1)}{1} \cdot \frac{1}{x+1}$$

$$\frac{(x+1)(x-1)}{1} \cdot \frac{1}{x-1}$$

$$\frac{(x+1)(x-1)}{1} \cdot \frac{1}{(x+1)(x-1)}$$

$$x+1 + (-x^2+1)$$

$$x+1 + x^2-1$$

$$\frac{-x^2+x}{x^2+x} \rightarrow \frac{x(-x+1)}{x(x+1)}$$

$$\frac{-x+1}{x+1} \rightarrow \frac{-(x-1)}{x+1}$$

Simplify

$$27. \frac{\frac{4x}{x^2-4} - \frac{5}{x-2}}{\frac{2}{x-2} + \frac{3}{x+2}}$$

$$\text{clicker} = \text{LCD} = \frac{(x+2)(x-2)}{1}$$

$$\frac{\frac{4x}{\cancel{(x+2)\cancel{(x-2)}}}}{\cancel{(x+2)\cancel{(x-2)}}} - \frac{\frac{5}{\cancel{x-2}}}{\cancel{(x+2)\cancel{(x-2)}}} + \frac{\frac{2}{\cancel{(x+2)\cancel{(x-2)}}}}{\cancel{x-2}} + \frac{\frac{3}{\cancel{x+2}}}{\cancel{(x+2)\cancel{(x-2)}}}$$

$$\frac{4x - 5(x+2)}{2(x+2) + 3(x-2)} \rightarrow \frac{4x - 5x - 10}{2x + 4 + 3x - 6}$$

$$\rightarrow \frac{-x - 10}{5x - 2}$$

Simplify

$$29. \frac{\frac{2y}{y^2 + 4y + 3}}{\frac{1}{y+3} + \frac{2}{y+1}}$$

$$\frac{2y}{(y+3)(y+1)} \div \left(\frac{1}{y+3} + \frac{2}{y+1} \right)$$

$$\frac{2y}{(y+3)(y+1)} \div \frac{y+1 + 2y+6}{(y+3)(y+1)}$$

$$\frac{2y}{(y+3)(y+1)} \cdot \frac{(y+3)(y+1)}{3y+7}$$

$$\frac{2y}{3y+7}$$

$$42. \frac{\frac{1}{x+1}}{x - \frac{1}{x}}$$

$$\frac{1}{x+1}$$

$$x - \frac{1}{x}$$

$\downarrow \div \frac{x^2+1}{x}$
 $\downarrow \cdot \frac{x}{x^2+1}$

$$\frac{1}{x+1} \cdot \frac{x}{x^2+1} = \frac{x}{(x+1)(x^2+1)}$$

$$x^3 + x - x$$

$$x^2 + 1$$

$\rightarrow \frac{1}{(x+1)} \cdot \frac{x^2+1}{x^3}$

$$\frac{x^2+1}{x^3(x+1)}$$

$$\frac{3x^2y}{11} \rightarrow \frac{3y}{x^2}$$

$$26. \frac{5a^{-1} - 2b^{-1}}{25a^{-2} - 4b^{-2}}$$

$$\frac{\frac{a^2}{b} \cdot 5}{1 \cdot a} - \frac{2 \cdot \frac{a^2}{b}}{b \cdot 1} \rightarrow \frac{5ab^2 - 2a^2b}{25b^2 - 4a^2}$$

$$\frac{\frac{a^2}{b^2} \cdot 25}{1 \cdot a^2} - \frac{4 \cdot \frac{a^2}{b^2}}{b^2 \cdot 1} \rightarrow \frac{ab(5b - 2a)}{(5b + 2a)(5b - 2a)} \rightarrow \frac{ab}{5b + 2a}$$

Simplify

8. $\frac{12x^{-2} - 3x^{-1}}{15x^{-1} - 9x^{-2}}$

1

$$\frac{\frac{12}{x^2} - \frac{3}{x}}{\frac{15}{x} - \frac{9}{x^2}} \rightarrow \frac{12 - 3x}{15x - 9}$$

$$\frac{3(4-x)}{3(5x-3)}$$

Simplify:

18. $(x^{-1} + y^{-1})^{-1}$

$$\left(\frac{1}{x} + \frac{1}{y}\right)^{-1}$$

$\xrightarrow{\text{LCD } xy}$

$$\frac{\frac{xy}{x} + \frac{xy}{y}}{xy}$$

$$\frac{y + x}{xy}$$